

Why Do Emerging Economies Borrow in Foreign Currency? The Role of Exchange Rate Risk

Annie Lee

Johns Hopkins SAIS

annie.lee.econ@gmail.com

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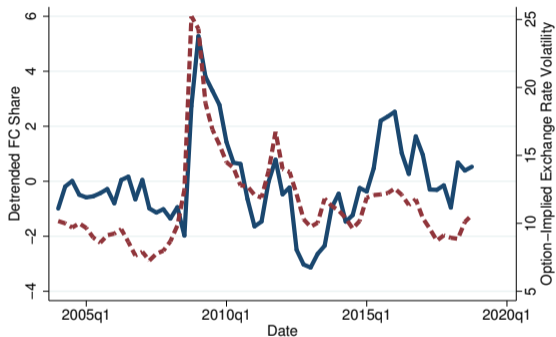
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- Now, EMs gained credibility in their monetary policy and started borrowing from abroad in LC.
- Nonetheless, EM govts **still borrow substantially in FC**.
 - The average FC share of external sovereign debt in emerging economies is 80% in 2004 – 2018.

The currency composition shifts more to FC when it is riskier to do so

- In fact, emerging economies borrow *even more* in FC than in LC when exchange rate volatility \uparrow .



— Detrended FC Share of External Public Debt (%)

- - - Option-Implied Exchange Rate Volatility (%)

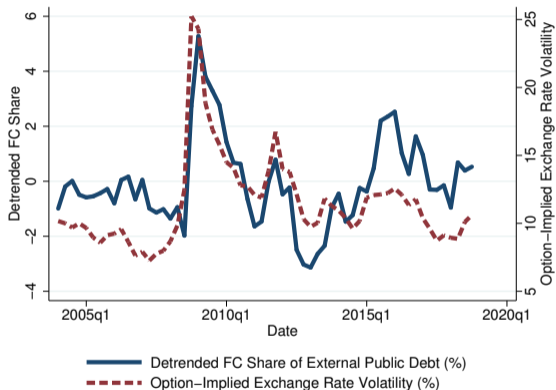
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▶ FX-Adjusted

▶ LC Share Trend

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- High positive correlation between FC share and exchange rate volatility: 0.65

1. Why do emerging market sovereigns still borrow substantially in FC?
2. Why do they borrow *even more* in FC than in LC when exchange rate volatility is *higher*?
3. How large is the welfare gain from exchange rate stabilization?

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- The currency composition of EM external sovereign debt is the outcome of choosing **how much risk EM sovereign bears oneself & how much risk it shifts to foreign investors**.
 - cheap but risky FC debt**
 - expensive but not risky LC debt**

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- The currency composition of EM external sovereign debt is the outcome of choosing **how much risk EM sovereign bears oneself & how much risk it shifts to foreign investors**.
 - cheap but risky FC debt**
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- When the **risk aversion** of international lenders is high, EM borrows substantially in FC & bears exchange rate risk because borrowing in LC is expensive.

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- EM borrows even more in FC as FX volatility \uparrow since it is even more expensive to borrow in LC.

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- ★ This paper captures how one asset can be **risky to one agent but not to the other** as their preferences concern their consumption evaluated in different units (\neq many open macro models w/ PPP or a single good)

Currency Composition of Sovereign Debt

- Monetary policy commitment:

Ottonello, Perez (2019), Engel, Park (2018), Du, Pfluger, Schreger (2021)

FX Risk Premium

- Many papers are devoted to explain Fama (1984) puzzle.

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★ This paper bridges the two literatures:

- (1) Documents **two new empirical relationships:**

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(ii) When FX volatility \uparrow , the cost of borrowing in LC relative to FC \uparrow

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- (4) Measure the **welfare gain** of stabilizing the exchange rate.
 - ◇ The welfare gain for the EM sovereign of shutting down the exchange rate volatility to zero is **0.35% in c.e.**

Empirical Analysis

- 18 EM countries in 2004 – 2018:
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- I run two sets of panel regressions & establish two empirical patterns.

$$\text{FC Share}_{it} = \beta_1 \sigma_{FX,it} + \Gamma' X_{it} + \gamma_i + \epsilon_{it}$$

- Country i , quarterly date t .
- Cyclical component of the external public debt in FC, FC Share_{it} .

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EM borrows relatively more in FC as FX volatility increases

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- Macro variables X_{it} are included: **expected depreciation**, **inflation**, **real GDP growth**, capital control index, private credit/GDP, external public debt/GDP, default prob.

EM borrows relatively more in FC as FX volatility increases

- FC Share_{it}: detrended FC Share of the public external debt.

$$\text{FC Share}_{it} = \beta_1 \sigma_{FX,it} + \Gamma' X_{it} + \gamma_i + \epsilon_{it}$$

| | Detrended FC Share of Public External Debt (%) | | | |
|------------------------|--|---------------------|---------------------|---------------------|
| $\sigma_{FX,IMPLIED}$ | 0.321*** (0.054) | 0.324*** (0.058) | | |
| $\sigma_{FX,REALIZED}$ | | | 0.310*** (0.057) | 0.331*** (0.061) |
| Macro Controls | No | Yes | No | Yes |
| R^2 | 0.095 | 0.128 | 0.102 | 0.140 |
| N | 909 | 793 | 982 | 862 |

* Driscoll and Kraay (1998) standard errors are reported in the parentheses.

X_{it} : expected depreciation, inflation, real GDP growth, capital control index, private credit/GDP, external public debt/GDP, default prob.

Robust to (1) post-GFC sample [▶ PostGFC](#), (2) FX-adjusted FC Share of external public debt [▶ FXadj](#), (3) controlling global factors. [▶ GlobalControls](#), (4) Time FE [▶ TimeFE](#), (5) linear-detrending [▶ LinearDetrending](#)

Relative cost of borrowing in LC over FC increases with higher FX volatility

$$\underbrace{y_{i,t}^{LC}}_{\text{one-year LC interest rate}} - \underbrace{(y_{i,t}^{FC} + s_{i,t+12} - s_{i,t})}_{\text{one-year FC interest rate in units of LC}} = \alpha_1 \sigma_{FX,it} + \Omega' X_{it} + \omega_i + \omega_t + \epsilon_{it}$$

- country i , monthly date t .
- LC one-year interest rate y_{it}^{LC} : 1-year zero coupon LC yields from Bloomberg Fair Value Curve
- FC one-year interest rate y_{it}^{FC} : 1-year USD denominated CDS spread + US 1-year treasury rate
Du, Pflueger, Schreger (2021)
- $s_{i,t}$ is the log of the exchange rate, defined as LC price of dollar.

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| | Relative Cost of Borrowing in LC over FC (%) | | | |
|------------------------|--|---------------------|---------------------|--------------------|
| $\sigma_{FX,IMPLIED}$ | 0.894*** (0.178) | 0.659*** (0.192) | | |
| $\sigma_{FX,REALIZED}$ | | | 0.664*** (0.196) | 0.450** (0.222) |
| Macro Controls | No | Yes | No | Yes |
| R^2 | 0.613 | 0.655 | 0.603 | 0.647 |
| N | 1768 | 1587 | 1866 | 1680 |

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X_{it} : **expected depreciation**, **inflation**, **real GDP growth**, capital control index, private credit/GDP, external public debt/GDP, default prob.

▶ Figure

▶ Separate

▶ Ex-ante

Model

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- Endowment and exchange rate shocks are correlated:

$$\begin{pmatrix} \log(y_t) \\ \log(S_t) \end{pmatrix} = \begin{pmatrix} \mu_y \\ \mu_s \end{pmatrix} + \begin{pmatrix} \rho_y & 0 \\ 0 & \rho_s \end{pmatrix} \begin{pmatrix} \log(y_{t-1}) \\ \log(S_{t-1}) \end{pmatrix} + \begin{pmatrix} \epsilon_t^y \\ \epsilon_t^s \end{pmatrix} \quad \text{where} \quad \begin{pmatrix} \epsilon_t^y \\ \epsilon_t^s \end{pmatrix} \sim N \left(\begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_y^2 & \rho_{y,s}\sigma_y\sigma_s \\ \rho_{y,s}\sigma_y\sigma_s & \sigma_s^2 \end{pmatrix} \right)$$

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- Sovereign default cost shocks are not correlated with other shocks:

$$\nu_t = \mu_\nu + \rho_\nu \nu_{t-1} + \epsilon_t^\nu, \quad \text{where} \quad \epsilon_t^\nu \sim N(0, \sigma_\nu^2)$$

as in Arellano, Bai, Bocola (2019) and Arellano, Bai, Mihalache (2018)

- Maximizes the expected life-time utility and has a CRRA utility with risk aversion γ .

$$U_t = \mathbb{E}_t \sum_{j=t}^{\infty} \beta^{j-t} (u(c_j) - D_j \nu_j)$$

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- b_{t+1}^{LC} and b_{t+1}^{FC} denote how much the sovereign borrows in LC and in FC.
- S_t is the LC price of dollar.
- When the sovereign does not default, the period budget constraint is:

$$c_t + b_t^{LC} + b_t^{FC} S_t = q_t^{LC} b_{t+1}^{LC} + q_t^{FC} b_{t+1}^{FC} S_t + y_t$$

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$$c_t = q_t^{LC} b_{t+1}^{LC} + q_t^{FC} b_{t+1}^{FC} S_t + y_t$$

- Risk-averse investors endowed with 1 unit of FC every period, taking the price of debt as given.
- CRRA utility with risk-aversion α , with second order Taylor approximation, equivalent of maximizing mean-variance of one-period return.
- Each investor maximizes mean-variance utility over their portfolio returns in units of FC.

$$\max_{B_{t+1}^{FC} \geq 0, B_{t+1}^{LC} \geq 0} \mathbb{E}_t(\tilde{R}_{t+1}) - \frac{\alpha}{2} \text{Var}_t(\tilde{R}_{t+1})$$

Risk-averse Foreign Investors

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$$\tilde{R}_{t+1} = \underbrace{(1 - B_{t+1}^{FC} - B_{t+1}^{LC})(1 + r_f)}_{\text{US treasury}} + \underbrace{\frac{B_{t+1}^{FC}}{q_t^{FC}}(1 - D_{t+1})}_{\text{EM FC debt}} + \underbrace{\frac{B_{t+1}^{LC}}{q_t^{LC}} \left(\frac{S_t}{S_{t+1}} (1 - D_{t+1}) \right)}_{\text{EM LC debt}}$$

▶ Markov Perfect Equilibrium

▶ Mechanism

Quantitative Analysis

- One period is a year, calibrated to Colombia in 2004–18.

| Parameters | Description | Values | Notes |
|--|--|--------|------------------------------|
| Parameters from the literature | | | |
| γ | Risk aversion of the sovereign | 1.0 | Literature |
| Parameters from the data | | | |
| ρ_y | Persistence of output shock | 0.9 | AR(1), Colombia |
| σ_y | Std of output shock | 0.03 | AR(1), Colombia |
| ρ_s | Persistence of exchange rate shock | 0.99 | AR(1), Colombia |
| σ_s | Std of exchange rate shock | 0.13 | AR(1), Colombia |
| $\rho_{y,s}$ | Correlation of output and exchange rate shocks | -0.11 | AR(1), Colombia |
| r_f | Risk-free rate | 0.5% | mean 5-year US real rate |
| Parameters from moment matching | | | |
| β | Time discount factor | 0.93 | External Debt to GDP (14.8%) |
| α | Risk aversion of the global investors | 51 | mean LC spread (1.63%) |
| μ_ν | Mean sovereign default cost | 0.59 | mean FC spread (0.66%) |
| σ_ν | Std sovereign default cost | 0.16 | std FC spread (0.54%) |

- The spread is against the US treasury taking into account of inflation.
- c.f. Hatchondo, Martinez and Sosa-Padilla (JPE, 2016), $\gamma = 2$, $\alpha = 59$.

Quantitative Model: Targeted and Untargeted Moments

| | Data | Model |
|---------------------------|------|-------|
| | % | % |
| <u>Targeted moments</u> | | |
| Mean LC Spread | 1.63 | 1.63 |
| Mean FC Spread | 0.66 | 0.64 |
| Std of FC Spread | 0.54 | 0.53 |
| Mean External Debt to GDP | 14.8 | 13.2 |
| <u>Untargeted moments</u> | | |
| Mean FC Share | 82.0 | 86.7 |
| Std of LC Spread | 2.30 | 2.00 |

Counterfactual Analysis

Experiment # 1: Higher FX Volatility

- Increase the FX volatility from 13% to 14%.
- Compute how the mean of the following variables have changed:
 - (i) FC share of external debt
 - (ii) Relative cost of borrowing in LC over FC: $y_{i,t}^{LC} - (y_{i,t}^{FC} + s_{i,t+12} - s_{i,t})$
- Compare them with the data counter-part: **untargeted moments**.

Untargeted Moments

- With higher FX volatility, the relative cost of borrowing in LC over FC increases.
- With higher FX risk premium, the sovereign shifts its currency composition towards FC.

| | Baseline $\sigma_s = 13\%$ | Counterfactual Higher $\sigma_s = 14\%$ | Higher FX Volatility $\Delta\sigma_s = +1\%$ | |
|---|-------------------------------|--|---|------------------|
| | | | Δ in Model | Δ in Data |
| Relative cost: $y_t^{LC} - (y_t^{FC} + s_t - s_{t+12})$ | 0.99% | 1.30% | +0.31% | +0.45% |
| FC Share | 86.70% | 87.07% | +0.37% | +0.33% |

▶ LargerIncreaseFXVol

▶ LargerDecreaseFXVol

Experiment # 2: Measuring Welfare Cost of Currency Mismatch

- Drive down the exchange rate volatility to zero: LC and FC debt are perfect substitutes.
- Compute the welfare gain for the EM sovereign of removing exchange rate volatility.

Rationalizing Fear of Floating

When there is no exchange rate shock ($\sigma_S = 0$),

- The interest rate spread goes down.
- The welfare gain, measured as the consumption equivalence, is 0.35%.
- It rationalizes the fear of floating even when emerging market can borrow in their own currencies.

| | Baseline | $\sigma_S = 0$ |
|----------------|----------|----------------|
| Relative cost | 0.99% | 0% |
| $y^{LC} - r_f$ | 1.63% | 0.57% |
| $y^{FC} - r_f$ | 0.66% | 0.57% |
| Welfare | | +0.35% c.e. |

- This paper documents two new empirical facts:
 - (i) a positive co-movement between FX volatility and FC share.
 - (ii) a positive co-movement between FX volatility and the relative cost of borrowing in LC over FC.

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- This paper highlights how the **currency mismatch on lenders** determines the FX risk-premium and the currency composition of EM external sovereign debt.
- The welfare cost of the exchange rate risk sheds light on the optimal exchange rate policy.

THANK YOU!

annie.lee.econ@gmail.com

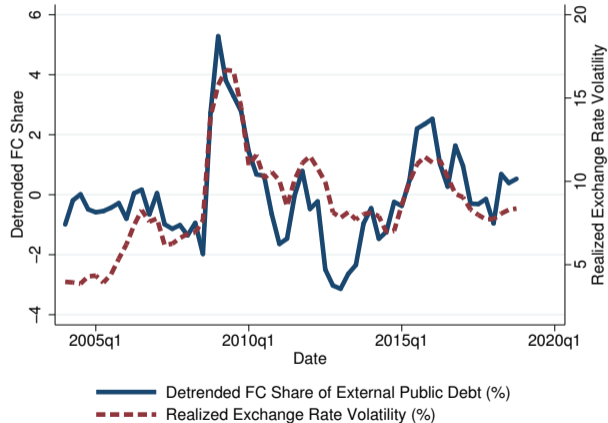
Appendix

#2 with alternative FX volatility measure: Figure

- **Alternative FX volatility** measure:

Annualized volatility of daily exchange rate returns against \$ in the past 4 quarters.

▶ Back



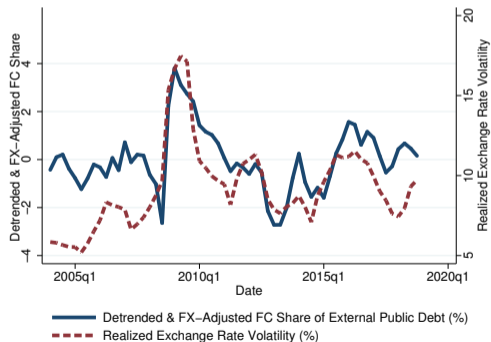
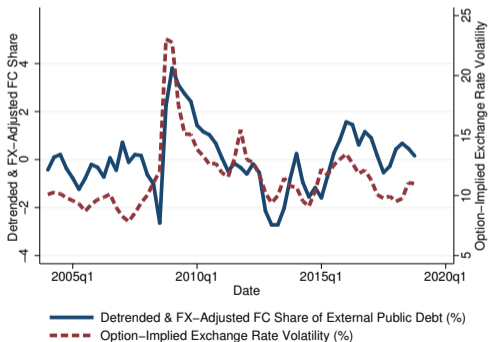
#2 with FX-adjusted measure of FC share: Figures

- FX-adjusted measure of FC Share is used:

$$\text{FC Share}_{it} = \frac{S_{i,2006Q1} F_{it}}{D_{it} + S_{i,2006Q1} F_{it}}$$

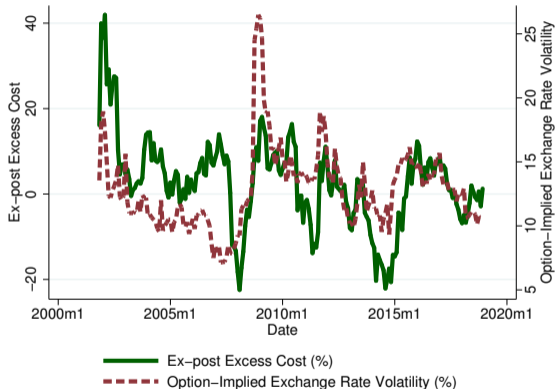
[▶ Back](#)

LHS: Implied FX Volatility, RHS: Realized FX Volatility



Relative Cost of Borrowing in LC over FC \uparrow as FX volatility \uparrow

- The relative cost of borrowing in LC over FC increases with higher exchange rate volatility.
- The required FX risk premium \uparrow as the exchange rate risk that lenders bear \uparrow .



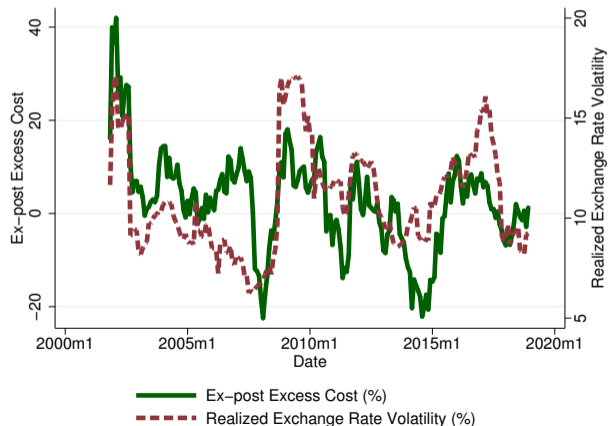
► Alt.FX Risk Measure

- There is a positive correlation of 0.4.

► Back

#1 with alternative FX volatility measure : Figure

- Dependent variable is: $y_{i,t}^{LC}$ — $(y_{i,t}^{FC} + s_{i,t+12} - s_{i,t})$ for country i at month t .
Cost of Borrowing in LC Cost of Borrowing in FC in units of LC
- The correlation in the whole sample is 0.4. [▶ Back](#)



EM borrows relatively more in FC as FX volatility increases

- Post-GFC sample period

▶ Back

$$\text{FC Share}_{it} = \beta_1 \sigma_{FX,it} + \Gamma' X_{it} + \gamma_i + \epsilon_{it}$$

| | Detrended FC Share of Public External Debt (%) | |
|------------------------|--|---------------------|
| $\sigma_{FX,IMPLIED}$ | 0.428*** (0.059) | |
| $\sigma_{FX,REALIZED}$ | | 0.333*** (0.044) |
| Macro Controls | Yes | Yes |
| R^2 | 0.204 | 0.187 |
| N | 593 | 629 |

* Driscoll and Kraay (1998) standard errors are reported in the parentheses.

X_{it} : expected depreciation, inflation, real GDP growth, capital control index, private credit/GDP external public debt/GDP, default prob.

EM borrows relatively more in FC as FX volatility increases

- FX-adjusted FC Share:

▶ Back

$$\text{FX-adj FC Share}_{it} = \frac{S_{i,2006Q1} F_{it}}{D_{it} + S_{i,2006Q1} F_{it}}$$

$$\text{FX-adj FC Share}_{it} = \beta_1 \sigma_{FX,it} + \Gamma' X_{it} + \gamma_i + \epsilon_{it}$$

| | Detrended FC Share of Public External Debt (%) | |
|------------------------|--|--------------------|
| $\sigma_{FX,IMPLIED}$ | 0.167*** (0.046) | |
| $\sigma_{FX,REALIZED}$ | | 0.164** (0.065) |
| Macro Controls | Yes | Yes |
| R^2 | 0.069 | 0.067 |
| N | 793 | 862 |

* Driscoll and Kraay (1998) standard errors are reported in the parentheses.

X_{it} : expected depreciation, inflation, real GDP growth, capital control index, private credit/GDP external public debt/GDP, default prob.

EM borrows relatively more in FC as FX volatility increases

- Control global factors: VIX Index, the 10-Year Treasury yield, the TED spread, and the US Federal Funds Rate. [▶ Back](#)

$$\text{FC Share}_{it} = \beta_1 \sigma_{FX,it} + \Gamma' X_{it} + GC_t + \gamma_i + \epsilon_{it}$$

| | Detrended FC Share of Public External Debt (%) | |
|------------------------|--|---------------------|
| $\sigma_{FX,IMPLIED}$ | 0.405*** (0.079) | |
| $\sigma_{FX,REALIZED}$ | | 0.334*** (0.064) |
| Macro Controls | Yes | Yes |
| R^2 | 0.162 | 0.164 |
| N | 793 | 862 |

* Driscoll and Kraay (1998) standard errors are reported in the parentheses.

X_{it} : expected depreciation, inflation, real GDP growth, capital control index, private credit/GDP external public debt/GDP, default prob.

EM borrows relatively more in FC as FX volatility increases

- Include quarterly time FE.

▶ Back

$$\text{FC Share}_{it} = \beta_1 \sigma_{FX,it} + \Gamma' X_{it} + \gamma_i + \gamma_t + \epsilon_{it}$$

| | Detrended FC Share of Public External Debt (%) | |
|------------------------|--|---------------------|
| $\sigma_{FX,IMPLIED}$ | 0.263*** (0.077) | |
| $\sigma_{FX,REALIZED}$ | | 0.180*** (0.048) |
| Macro Controls | Yes | Yes |
| R^2 | 0.285 | 0.264 |
| N | 861 | 934 |

* Driscoll and Kraay (1998) standard errors are reported in the parentheses.

X_{it} : expected depreciation, inflation, real GDP growth, capital control index, private credit/GDP external public debt/GDP, default prob.

EM borrows relatively more in FC as FX volatility increases

- Linear detrending.

▶ Back

$$\text{FC Share}_{it} = \beta_1 \sigma_{FX,it} + \Gamma' X_{it} + \gamma_i + \gamma_t + \epsilon_{it}$$

| | Detrended FC Share of Public External Debt (%) | |
|------------------------|--|--------------------|
| $\sigma_{FX,IMPLIED}$ | 0.278*** (0.083) | |
| $\sigma_{FX,REALIZED}$ | | 0.227** (0.107) |
| Macro Controls | Yes | Yes |
| R^2 | 0.088 | 0.089 |
| N | 745 | 814 |

* Driscoll and Kraay (1998) standard errors are reported in the parentheses.

X_{it} : expected depreciation, inflation, real GDP growth, capital control index, private credit/GDP external public debt/GDP, default prob.

Result # 1: Relative cost of borrowing in LC over FC increases with higher FX volatility.

$$y_{it}^j = \gamma_1 \sigma_{FX,it} + \Theta' X_{it} + \theta_i + \theta_t + e_{it}, \text{ where } j = \{LC, FC\}$$

| Dependent Variable: | LC interest Rate | FC interest rate | LC interest Rate | FC interest rate |
|------------------------|---------------------|---------------------|---------------------|------------------|
| $\sigma_{FX,IMPLIED}$ | 0.224*** (0.024) | 0.080*** (0.022) | | |
| $\sigma_{FX,REALIZED}$ | | | 0.147*** (0.025) | 0.009 (0.009) |
| Macro Controls | Yes | Yes | Yes | Yes |
| R^2 | 0.631 | 0.871 | 0.627 | 0.846 |
| N | 2437 | 1745 | 2575 | 1980 |

* Driscoll and Kraay (1998) standard errors are reported in the parentheses.

X_{it} : expected depreciation, inflation, real GDP growth, capital control index, private credit/GDP, external public debt/GDP default prob.

Relative cost of borrowing in LC over FC increases with higher FX volatility.

$$\underbrace{y_{i,t}^{LC}}_{\text{one-year LC interest rate}} - \underbrace{(y_{i,t}^{FC} + E_t(s_{i,t+12} - s_{i,t}))}_{\text{one-year FC interest rate in units of LC}} = \alpha_1 \sigma_{FX,it} + \Omega' X_{it} + \alpha_i + \alpha_t + \epsilon_{it}$$

| Dependent Variable: | Relative Cost of Borrowing in LC over FC (%) | | | |
|------------------------|--|--------------------|--------------------|---------------------|
| $\sigma_{FX,IMPLIED}$ | 0.114** (0.052) | 0.113** (0.048) | | |
| $\sigma_{FX,REALIZED}$ | | | 0.103** (0.044) | 0.087*** (0.033) |
| Country FE | Yes | Yes | Yes | Yes |
| Time FE | Yes | Yes | Yes | Yes |
| Macro Controls | No | Yes | No | Yes |
| R^2 | 0.365 | 0.869 | 0.359 | 0.870 |
| N | 1768 | 1587 | 1866 | 1680 |

* Driscoll and Kraay (1998) standard errors are reported in the parentheses.

X_{it} : expected depreciation, inflation, real GDP growth, capital control index
private credit/GDP, external public debt/GDP, default prob.

Discussion of Assumption: Myopic Investors

1. In the real world, quarterly/annual regulatory requirements on institutional investors.
2. For tractability, no need to carry investors' aggregate wealth as an additional state variable.
3. Allow an analytical illustration of the mechanism.

▶ Back

Recursive Problem of EM Sovereign Borrower

- $X = \{y, S, \nu\}$ is a set of exogenous states.
- **Sovereign** maximizes:

$$V(b^{LC}, b^{FC}; X) = \max_{c \geq 0, b'^{LC}, b'^{FC}} \{u(c) + \beta E_{X'|X} W(b'^{LC}, b'^{FC}; X')\}$$

$$c + b^{LC} + b^{FC} S = q^{LC}(b'^{LC}, b'^{FC}; X) b'^{LC} + q^{FC}(b'^{LC}, b'^{FC}; X) b'^{FC} S + y$$

Recursive Problem of EM Sovereign Borrower

- $X = \{y, S, \nu\}$ is a set of exogenous states.
- **Sovereign** maximizes:

$$V(b^{LC}, b^{FC}; X) = \max_{c \geq 0, b'^{LC}, b'^{FC}} \{u(c) + \beta E_{X'|X} W(b'^{LC}, b'^{FC}; X')\}$$

$$c + b^{LC} + b^{FC} S = q^{LC}(b'^{LC}, b'^{FC}; X) b'^{LC} + q^{FC}(b'^{LC}, b'^{FC}; X) b'^{FC} S + y$$

- **Sovereign** chooses to default ($D = 1$) or not ($D = 0$):

$$W(b^{LC}, b^{FC}; X) = \max_{D=\{0,1\}} \{(1-D)V(b^{LC}, b^{FC}; X) + D[V(0, 0; X) - \underbrace{\nu}_{\text{Default Disutility Costs}}]\}$$

- State variables are:

$$\{b^{LC}, b^{FC}; X\}$$

- Choice variables are:

$$D(b^{LC}, b^{FC}; X), b'^{LC}(b^{LC}, b^{FC}; X), b'^{FC}(b^{LC}, b^{FC}; X)$$

- Bond markets clear:

$$b'^{LC} = B'^{LC} \cdot S, \quad b'^{FC} = B'^{FC}$$

- Bond price schedules:

$$q^{LC}(b'^{LC}, b'^{FC}; X), q^{FC}(b'^{LC}, b'^{FC}; X)$$

Mechanism

As FX volatility \uparrow , Relative Price of FC over LC debt \uparrow

- Assume there is no default risk $D_{t+1} = 0$.
- The relative price of FC over LC debt:

$$q_t^{FC} - q_t^{LC} = \frac{1}{1+r_f} - \underbrace{\frac{\mathbb{E}_t\left(\frac{S_t}{S_{t+1}}\right)}{1+r_f}}_{q_{RN,t}^{LC} : \text{Risk Neutral LC Bond Price}} \times \underbrace{\left(\frac{1}{2} + \frac{1}{2} \sqrt{1 - 4B^{LC}(1+r_f)\alpha \underbrace{\text{Var}_t\left(\frac{S_t}{S_{t+1}}\right)}_{\propto \sigma_S^2}} \right)}_{\Psi_t^{LC} : \text{Risk Premium on LC Bond} < 1}$$

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- Relative price of FC over LC debt increases with $\sigma_S^2 \uparrow$,
i.e. **the interest rate on LC over FC debt is higher with $\sigma_S^2 \uparrow$:**

$$\frac{\partial(q^{FC} - q^{LC})}{\partial \sigma_S^2} > 0$$

As FX volatility \uparrow , Relative Price of FC over LC debt \uparrow

- Assume there is no default risk $D_{t+1} = 0$.
- The relative price of FC over LC debt:

$$q_t^{FC} - q_t^{LC} = \frac{1}{1+r_f} - \underbrace{\frac{\mathbb{E}_t\left(\frac{S_t}{S_{t+1}}\right)}{1+r_f}}_{q_{RN,t}^{LC} : \text{Risk Neutral LC Bond Price}} \times \underbrace{\left(\frac{1}{2} + \frac{1}{2} \sqrt{1 - 4B^{LC}(1+r_f)\alpha \underbrace{\text{Var}_t\left(\frac{S_t}{S_{t+1}}\right)}_{\propto \sigma_S^2}} \right)}_{\Psi_t^{LC} : \text{Risk Premium on LC Bond} < 1}$$

- Relative price of FC over LC debt increases with $\sigma_S^2 \uparrow$,
i.e. **the interest rate on LC over FC debt is higher with $\sigma_S^2 \uparrow$:**

$$\frac{\partial(q^{FC} - q^{LC})}{\partial \sigma_S^2} > 0$$

- The increase is larger as the risk aversion of lender α , is larger.

As FX volatility \uparrow , Relative Price of FC over LC debt \uparrow

- Assume there is no default risk $D_{t+1} = 0$.
- The relative price of FC over LC debt:

$$q_t^{FC} - q_t^{LC} = \frac{1}{1+r_f} - \underbrace{\frac{\mathbb{E}_t\left(\frac{S_t}{S_{t+1}}\right)}{1+r_f}}_{q_{RN,t}^{LC} : \text{Risk Neutral LC Bond Price}} \times \underbrace{\left(\frac{1}{2} + \frac{1}{2} \sqrt{1 - 4B^{LC}(1+r_f)\alpha \underbrace{\text{Var}_t\left(\frac{S_t}{S_{t+1}}\right)}_{\propto \sigma_S^2}} \right)}_{\Psi_t^{LC} : \text{Risk Premium on LC Bond} < 1}$$

- Relative price of FC over LC debt increases with $\sigma_S^2 \uparrow$,
i.e. **the interest rate on LC over FC debt is higher with $\sigma_S^2 \uparrow$:**

$$\frac{\partial(q^{FC} - q^{LC})}{\partial \sigma_S^2} > 0$$

- The increase is larger as the risk aversion of lender α , is larger.
- Specifically, when $\alpha = 0$,

$$q_t^{FC} - q_t^{LC} = \frac{1}{1+r_f} - \frac{\mathbb{E}_t\left(\frac{S_t}{S_{t+1}}\right)}{1+r_f} \implies \frac{\partial(q^{FC} - q^{LC})}{\partial \sigma_S^2} = 0 \ll 0.4 \text{ (Data)}$$

As FX volatility \uparrow , EM borrows more in FC

- Assume there is no default risk $D_{t+1} = 0$ and $E_t \left(\frac{S_{t+1}}{S_t} \right) = 1$.
- Then, EM's currency composition of external borrowing will be determined by:

$$u'(c_t) \underbrace{\left[q_t^{FC} - \left(q_t^{LC} + \frac{\partial q_t^{LC}}{\partial b_{t+1}^{LC}} \right) \right]}_{\text{MB of one more FC debt and one less LC debt}} = \underbrace{\beta \text{Cov} \left(u'(c_{t+1}), \frac{S_{t+1}}{S_t} \right)}_{\text{MC of one more FC debt and one less LC debt}}$$

As FX volatility \uparrow , EM borrows more in FC

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- With a large enough lenders' risk aversion α ,

$$\sigma_S^2 \uparrow \implies q^{FC} - q^{LC} \uparrow\uparrow$$

As FX volatility \uparrow , EM borrows more in FC

- Assume there is no default risk $D_{t+1} = 0$ and $E_t \left(\frac{S_{t+1}}{S_t} \right) = 1$.
- Then, EM's currency composition of external borrowing will be determined by:

$$u'(c_t) \underbrace{\left[q_t^{FC} - \left(q_t^{LC} + \frac{\partial q_t^{LC}}{\partial b_{t+1}^{LC}} \right) \right]}_{\text{MB of one more FC debt and one less LC debt}} = \underbrace{\beta \text{Cov} \left(u'(c_{t+1}), \frac{S_{t+1}}{S_t} \right)}_{\text{MC of one more FC debt and one less LC debt}}$$

- With a large enough lenders' risk aversion α ,

$$\sigma_S^2 \uparrow \implies q^{FC} - q^{LC} \uparrow\uparrow$$

- It implies then,

$$u'(c_t) \underbrace{\left[q_t^{FC} - \left(q_t^{LC} + \frac{\partial q_t^{LC}}{\partial b_{t+1}^{LC}} \right) \right]}_{\text{LC MORE EXPENSIVE} \uparrow\uparrow} = \underbrace{\beta \text{Cov} \left(u'(c_{t+1}), \frac{S_{t+1}}{S_t} \right)}_{\text{FC MORE RISKY} \uparrow}$$

- The sovereign **borrows more in FC and less in LC.** [▶ back](#)

Untargeted Moments : Higher FX Volatility

| Model With Default | Targeted $\sigma_s = 13\%$ | Counterfactual Higher $\sigma_s = 15\%$ | Higher FX Volatility $\Delta\sigma_s = +2\%$ | |
|---|-------------------------------|--|---|------------------|
| | | | Δ in Model | Δ in Data |
| Relative cost: $y_{i,t}^{LC} - (y_{i,t}^{FC} + s_{i,t} - s_{i,t+12})$ | 0.99% | 1.73% | +0.74% | +0.90% |
| FC Share | 86.70% | 87.3% | +0.60% | +0.66% |

▶ Back

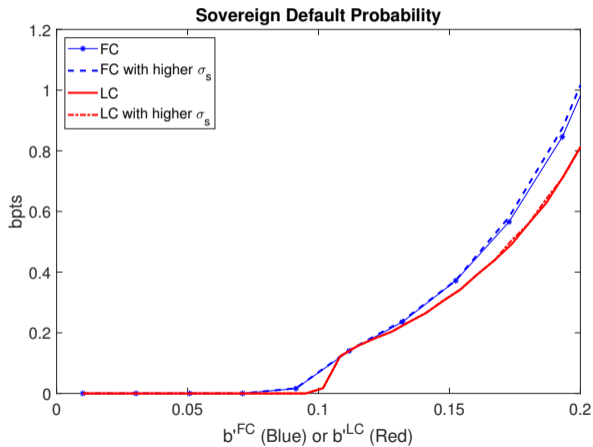
Untargeted Moments : Lower FX Volatility

| Model With Default | Targeted $\sigma_s = 13\%$ | Counterfactual Lower $\sigma_s = 11\%$ | Lower FX Volatility $\Delta\sigma_s = -2\%$ | |
|---|-------------------------------|---|--|------------------|
| | | | Δ in Model | Δ in Data |
| Relative cost: $y_{i,t}^{LC} - (y_{i,t}^{FC} + s_{i,t} - s_{i,t+12})$ | 0.99% | 0.73% | -0.27% | -0.90% |
| FC Share | 86.70% | 85.63% | -1.07% | -0.66% |

▶ Back

Model Mechanism: Default Probability with Higher σ_s

- The default prob. is slightly higher with higher exchange rate volatility for a given level of FC debt.



The other choice variable fixed at zero. Exogenous variables are held at their mean e.g. $S = 1$.